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INTERNAL REPORT

RECALCULATION OF THE WORK OF Ph. v. JOLLY ON THE DENSITY OF OXYGEN

BY

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INTERNAL REPORT

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RECALCULATION OF THE WORK OF Ph. v. JOLLY ON THE DENSITY OF OXYGEN "Die Veränderlichkeit in der Zusammensetzung der Atmosphärischen Luft"

Wiedemanns Annalen der Physik, Series (2), v. 6, pp. 520-544 (1879).

Abhandlungen der Mathematisch-Physikalischen Classe der Königlich
Bayerischen Akademie der Wissenschaften, v. 13, Part 2, pp. 51-74
(1880).

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RECALCULATION OF THE WORK OF Ph. v. JOLLY ON THE DENSITY OF OXYGEN

globe, of about 1 liter cap. By, filled with oxygen and then

weighing 10 grams. After the filling and evacuation, the

globe was completely covered with water so that it was

accurately at 0° C. The globe was evacuated to a pressure of 0.02

mm. Kg.

ABSTRACT

The volume of the globe was determined by weighing the amount of oxygen required to fill the globe to a pressure of 1 atmosphere. The original data of Ph. v. Jolly on the density of oxygen has been recalculated, using the latest values of the necessary physical constants. The value obtained is

$$\rho = 1.429054 \pm 22 \text{ g/l}$$

with $g = 980.616 \text{ cm/sec}^2$.

INTRODUCTION

The Helium Research Center is presently engaged in reviewing and recalculating all of the data that appear in the literature from which the value of the gas constant R is calculated. In this report I re-examined the work of Ph. v. Jolly on the determination of the density of oxygen at one atmosphere and at 0°C.

1/ Project Leader, Thermodynamics, Helium Research Center, Bureau of Mines, Amarillo, Texas.

Work on manuscript completed August 1964.

Ph. v. Jolly determined the density of oxygen by weighing a globe, of about 1 liter capacity, filled with oxygen and then weighing it evacuated. During the filling and evacuation, the globe was completely surrounded by ice and water so that it was accurately at 0° C. The globe was evacuated to a pressure of 0.02 mm Hg.

The volume of the globe was determined by weighing the amount of water that would fill the globe at 0° C.

Oxygen was prepared by electrolysis. The gas was freed of ozone and hydrogen by passing through a glass tube filled with glass chips and heated to a red heat. The gas was also passed over potassium hydroxide and phosphorous pentoxide.

DETERMINATION OF THE VOLUME OF Ph. v. JOLLY'S GLOBE

Ph. v. Jolly determined the volume of his globe by determining the weight of water that filled the volume. The fact that he corrected the weight of water for the weight of air displaced indicates that the weight of the empty globe must have been determined with the stopcock open to the atmosphere. Under these conditions the relationship for the weight of water in vacuum is given by

$$M_{H_2O} \left(1 - \frac{\rho_2}{\rho_{H_2O}}\right) = M_2 \left(1 - \frac{\rho_2}{\rho_w}\right) - M_1 \frac{\left(1 - \frac{\rho_1}{\rho_w}\right) \left(1 - \frac{\rho_2}{\rho_g}\right)}{\left(1 - \frac{\rho_1}{\rho_g}\right)} \quad (1)$$

In the above equation

M_{H_2O} = mass of water

M_2 = mass of weights on balance when globe filled with water

M_1 = mass of weights on balance when globe filled with air and open to the atmosphere

ρ_1 = density of air during weighing of globe when filled with air

ρ_2 = density of air during weighing of globe when filled with water

ρ_w = density of weights

ρ_g = average density of glass and stopcock in the globe

ρ_{H_2O} = density of water under conditions when the globe was weighed filled with water

$1 - \frac{\rho_2}{\rho_{H_2O}}$ is the buoyancy correction factor for the weight of air

displaced by the water. Ph. v. Jolly made this correction. $1 - \frac{\rho}{\rho_g}$

is the buoyancy correction factor for the weight of air displaced by the glass in the globe. As the ratio of two of these quantities is involved, the ratio only involves the change in the density of air between the two weighings. This correction is very small and was neglected by Ph. v. Jolly.

$1 - \frac{\rho}{\rho_w}$ is the buoyancy correction factor for the weight of air displaced by the weights. In his determination of the weight of water, Ph. v. Jolly applied this correction.

Since Jolly gives the temperature of the air and the barometric pressure, I have recalculated the weight of water applying all corrections. In these calculations, I have assumed the density of the glass as being $\rho_g = 2.6$ g/ml. Ph. v. Jolly gives the density of his weights as being $\rho_w = 8.4$ g/ml. I have calculated the density of air from the equation^{2/}.

2/ Barieau, Robert E.

The Density of Moist Air From 0° to Near 25° C and Near Atmospheric Pressure. Helium Research Center Internal Report No. 36, August 1963.

$$\rho = \rho_0 \frac{T_0}{T} P (1 - 0.37807y) \frac{Z_0}{Z} \quad (2)$$

In this equation

ρ is the density of air in g/liter

ρ_0 is the density of 0.04% CO_2 , dry air at 0° C and 1 atmosphere pressure

$\rho_0 = 1.2932$ g/liter

P is the pressure in atmospheres, where 1 atmosphere is 76 cm of Hg at 0° C and in a gravitational field of 980.665 cm/sec^2 in the Potsdam system.

T is the absolute temperature

T_0 is the absolute temperature of the ice point

y is the mole fraction of water vapor

Z_0 is the compressibility factor of 0.04% CO_2 , dry air at 0° C and 1 atmosphere

Z is the compressibility factor of the gas at P and T

$$\frac{Z_0}{Z} = 1 - 0.000602 (P - 1) + (0.00254y + 0.0758y^2)P - (0.0000105 + 0.0000131y + 0.00131y^2)tP \quad (3)$$

where in this equation, t is the temperature in $^\circ\text{C}$.

The mole fraction of water in air saturated with water vapor was taken as (3)

(3) Reference (2) page 17

$$y_{\text{sat}} = 1.0042 \frac{P_s}{P} \quad (4)$$

where P_s is the vapor pressure of pure water in atmospheres and P is the total atmospheric pressure in atmospheres. The vapor pressure of water was calculated from the equation given by Osborne, Stimson, and Ginnings (4)

(4) Osborne, N. S., H. F. Stimson, and D. C. Ginnings. Thermal Properties of Saturated Water and Steam. J. Research NBS, v. 23, 1939, pp. 261-270.

$$\log_{10} P_{\text{atm}} = -3.142305 \left[\frac{10^3}{T} - \frac{10^3}{373.16} \right] + 8.2 \log_{10} \frac{373.16}{T} \quad (5)$$

Using the equations given previously, I calculate for the vapor pressure of liquid water at 7.1°C

$$- 0.0024804 (373.16 - T)$$

The density of liquid water was taken from the table of Tilton and Taylor (5)

(5) Tilton, L. W., and J. K. Taylor. Accurate Representation of the Refractivity and Density of Distilled Water as a Function of Temperature. J. Research NBS, v. 18, 1937, pp. 205-214.

Ph. v. Jolly weighed his globe filled with air, with the stopcock open to the atmosphere, first on the right pan of his balance and then on the left pan. The two values were 142.074331 g and 142.072500 g with a geometric mean of 142.073415 g. Jolly adds to this 0.001876 as the sum of the corrections to his individual weights, giving

$$M_1 = 142.075291 \text{ g}$$

Atmospheric conditions during this weighing were $t = 7.1^{\circ}\text{C}$, $P = 721.57 \text{ mm Hg}$ at 0°C under local gravity. In correcting the atmospheric pressure to standard gravity, I used $g_{\text{local}} = 980.7361 \text{ cm/sec}^2$ and $g_{\text{standard}} = 980.665 \text{ cm/sec}^2$.

$$\text{Then } P = \frac{721.57 \times 980.7361}{760 \times 980.665} \text{ glass occupies } 54.7 \text{ ml.}$$

When filled with water at 0° C , the globe and water weighed 1150. $P = 0.949503$ atmospheres. 1150.292000 on the right pan

giving a gravitational pull of 1150.298380. To this, Jolly adds 0.000100 for the correction of the globe to give the vapor pressure of liquid water at 7.1° C .

$$P_s = 0.0099495 \text{ atmospheres.}$$

$$\text{Then } y_{\text{sat}} (7.1^\circ \text{ C}) = 1.0042 \times \frac{0.0099495}{0.949503}$$

$P = 721.3$ mm Hg 0° C (local gravity), hygrometer = 65%. I calculate

$$\text{or } y_{\text{sat}} = 0.0105226$$

Jolly does not give a hygrometer reading for this weighing, but he does give a value of 65% for the weighing when water was present in the globe. I will take a relative humidity of 65% for the first weighing also. I then calculate for the density of air vapor pressure of liquid water at 7.1° C

$$\rho_1 = 0.0011937 \text{ g/ml}$$

Then the true mass of the globe is

$$\frac{M_1 \left(1 - \frac{\rho_1}{\rho_w}\right)}{\left(1 - \frac{\rho_1}{\rho_g}\right)} = 142.075291 \frac{\left(1 - \frac{0.0011937}{8.4}\right)}{\left(1 - \frac{0.0011937}{2.6}\right)}$$

$$= 142.075291 \times \frac{0.9998578929}{0.9995408846}$$

$$= 142.120351 \text{ g}$$

and with a density of 2.6 the glass occupies 54.7 ml.

When filled with water at 0° C , the globe and water weighed 1150.304760 g on the left pan and 1150.292000 on the right pan giving a geometrical mean of 1150.298380. To this, Jolly adds 0.001302 for the calibration of his weights to give

$$M_2 = 1150.299682 \text{ g.}$$

During this weighing, atmospheric conditions were $t = 6.4^{\circ}\text{ C}$, $P = 721.3 \text{ mm Hg } 0^{\circ}\text{ C}$ (local gravity), hygrometer = 65%. I calculate

$$P = \frac{721.3}{760} \times \frac{980.7361}{980.665}$$

$$\text{give for the density } P = 0.949148 \text{ atmospheres.}$$

Using the equations given previously, I calculate for the vapor pressure of liquid water at 6.4° C

$$P_s = 0.0094821 \text{ atmospheres.}$$

Then

$$y(\text{sat}) (6.4^{\circ}\text{ C}) = 1.0042 \times \frac{0.0094821}{0.949148}$$

or

$$y(\text{sat}) = 0.0100321$$

and with the air 65% saturated with respect to water vapor, the mole fraction of water vapor then is

$$y = .65 \times .0100321 = 0.00652087.$$

Then with $t = 6.4^\circ \text{ C}$, $P = 0.949148$ atmospheres and $y = 0.00652087$, I calculate for the density of air ~~0.9995398462~~

$$\rho_2 = 0.0011964 \text{ g/ml.}$$

Tilton and Taylor (6)

(6) Reference 5, page 213

give for the density of water at 6.4° C

$$\rho_w = 0.9999546 \text{ g/ml}$$

Then the expression for the mass of water, M_{H_2O} , is given by

$$M_{H_2O} \left(1 - \frac{0.0011964}{0.9999546}\right) = 1150.299682 \left(1 - \frac{0.0011964}{8.4}\right)$$

$$-142.075291 \frac{\left(1 - \frac{0.0011937}{8.4}\right) \left(1 - \frac{0.0011964}{2.6}\right)}{\left(1 - \frac{0.0011937}{2.6}\right)}$$

or

DETERMINATION OF THE MASS OF OXYGEN

After finding the mass of water in the following way, he completely surrounded the globe with ice and water and admitted oxygen until the globe was ~~full~~ ^{1/2 full}. After equilibrium, the thermometer was read and the stopcock closed. The globe was then removed from the ice bath and weighed.

$$M_{H_2O} \times 0.9988035457 = 1150.299682 \times .9998575714$$

$$- 142.075291 \times \frac{0.9998578929}{0.9995408846} \times 0.9995398462$$

$$= 1150.135846 - 142.054953 = 1008.080893$$

It was then placed in the ice bath and evacuated to 0.02 mm of Hg, the stopcock

Then M_{H_2O} = 1009.288461 g. was weighed.

The weighing was carried out in the following way. Jolly had a tare globe that had the same external volume as his oxygen weighing globe, to within 0.06 ml. His weighing globe and tare which differs by 1.5 ppm from the value I have calculated.

Taking the density of water (7) and weights were necessary on

(7) Reference 5, page 213

at $0^\circ C$ as 0.9998676 g/ml, I calculate for the volume of Jolly's globe at $0^\circ C$

$$V = \frac{1009.288461}{0.9998676}$$

Let M_T be the mass of the tare globe and ice contents

$$V = 1009.4221 \text{ ml}$$

Let M_G be the mass of the globe to be filled with oxygen

or

Let V_T be the external volume of the tare globe during the

$$V = 1.0094221 \text{ liters}$$

Let V_G be the external volume at the time of weighing of the globe to be filled with oxygen

DETERMINATION OF THE MASS OF OXYGEN

Jolly determined the mass of oxygen in the following way. He completely surrounded the globe with ice and water and admitted oxygen until the globe was filled at atmospheric pressure. After equilibrium, the barometer was read and the stopcock closed. The globe was then removed and weighed. The globe was then returned to the ice bath and evacuated to 0.02 mm of Hg, the stopcock closed and the evacuated globe was weighed.

The weighings were carried out in the following way. Jolly had a tare globe that had the same external volume as his oxygen weighing globe, to within 0.06 ml. His weighing globe and tare globe were placed on the opposite pans of the balance. When his weighing globe was filled with oxygen, weights were necessary on the pan with the tare globe. When the weighing globe was evacuated, weights were necessary on the pan with the weighing globe. To correct for inequality of the balance arms, each weighing was done twice, interchanging the objects on the balance pans. Jolly applied corrections for the difference between the nominal value and actual value of his weights.

Let M_T be the mass of the tare globe and its contents

Let M_G be the mass of the globe to be filled with oxygen

Let V_T be the external volume of the tare globe during the weighing

Let V_G be the external volume at the time of weighing of the globe to be filled with oxygen

Let ρ_{air} be the density of the air at time of weighing

Let ρ_w be the density of the weights in the inside and outside

Let M_w be the mass of weights that bring the balance to equilibrium and may be expressed by

Let g be the mass of oxygen in the main globe.

Let the first weighing be with the main globe filled with oxygen.

When the balance is in equilibrium the following equation applies.

$$M_G + g_1 - V_{G_1} \rho_{air_1} = M_T - V_{T_1} \rho_{air_1} + M_w (1 - \frac{\rho_{air_1}}{\rho_w}) \quad (6)$$

Then

Let the second weighing be when the main globe is evacuated. Then at equilibrium

$$M_G + g_2 - V_{G_2} \rho_{air_2} + M_w (1 - \frac{\rho_{air_2}}{\rho_w}) = M_T - V_{T_2} \rho_{air_2} \quad (7)$$

Then

$$g_1 - g_2 = M_w (1 - \frac{\rho_{air_1}}{\rho_w}) + M_w (1 - \frac{\rho_{air_2}}{\rho_w}) \quad (8)$$

$$+ (V_{G_1} - V_{T_1}) \rho_{air_1} - (V_{G_2} - V_{T_2}) \rho_{air_2}$$

This equation includes all buoyancy corrections.

Jolly did not give the temperature, pressure, and relative humidity of the air during any of his weighings. We can only assume a constant value for the density of air. The necessity for making this correction was first

V_T and V_G will be a function of the temperature and also a function of the pressure difference between the inside and outside of the globe.

I assume this variation may be expressed by (London), v. 43,

1898, pp. 356-363.

$$V_T = (V_o + \delta)(1 + \alpha t) \quad (9)$$

$$(9) \quad V_G = V_o (1 + \alpha t) (1 + \beta \Delta P) \quad (10)$$

where ΔP is the pressure difference between inside and outside.

Then

$$V_G - V_T = V_o (1 + \alpha t) \beta \Delta P - \delta (1 + \alpha t) \quad (11)$$

For the first weighing, we assume $\Delta P = 0$. neglect this correction

Then determining the weight of the globe while in, as we have seen,

$$g_1 - g_2 = (M_{w1} + M_{w2}) (1 - \frac{\rho_{air}}{\rho_w}) \quad (12)$$

$$- V_o (1 + \alpha t_2) \beta \Delta P_2 \rho_{air}$$

where Lord Rayleigh, 'II On the Densities of the Principal Gases.'

$$\Delta P_2 = P_{inside} - P_{outside} \quad (13)$$

during the time of the weighing when the main globe is evacuated.

The correction term $V_o (1 + \alpha t_2) \beta \Delta P_2 \rho_{air}$ has been called the correction for the contraction of the globe. Jolly neglected this correction. The necessity for making this correction was first

pointed out by Lord Rayleigh (8)(9). Lord Rayleigh evidently

overlooked the fact that in weighing his water, Jolly used gold

(8) Lord Rayleigh. On the Relative Densities of Hydrogen and Oxygen. Preliminary Notice. Proc. Roy. Soc. (London), v. 43, together, 1888, pp. 356-363.

(9) Lord Rayleigh. On the Relative Densities of Hydrogen and Oxygen. Preliminary Notice. The Chemical News, v. 57, 1888, pp. 73-75.

The factor $(1 - \frac{\rho_{\text{air}}}{\rho_w})$ is the correction for air buoyancy on the weights. Ph. v. Jolly seems to have neglected this correction in determining the weight of his gases; while he, as we have seen, applied a buoyancy correction to his weights in determining the weight of water that filled his globe at 0° C. In regard to this point Lord Rayleigh says (10)

(10) Lord Rayleigh. II On the Densities of the Principal Gases.

Proc. Roy. Soc. (London), v. LIII, 1893, pp. 134-149. Footnote on page 140.

"In v. Jolly's calculations the buoyancy of the weights seems to be allowed for in dealing with the water, and neglected in dealing with the gases. If this be so, the result would be affected with a slight error which, however, far exceeds any that could arise

from neglecting buoyancy altogether." Lord Rayleigh evidently overlooked the fact that in weighing his water, Jolly used gold plated brass weights, while in weighing his gases, he used platinum weights. Under these conditions, neglecting buoyancy altogether introduces an error of 87 ppm low in the density of oxygen, while applying the buoyancy correction to the water determination and neglecting it in the determination of weight of gas, introduces an error of 56 ppm high in the density of oxygen. Applying both buoyancy corrections and assuming a 10% uncertainty in the density of air during the gas weight determinations, reduces the uncertainty in the density of oxygen to 5 ppm. I have therefore applied a buoyancy correction for the weights in the determination of the mass of oxygen. In these calculations, I have taken the density of air as being 0.0012 g/ml.

I reproduce below the data on the weight of oxygen given by Jolly in his paper.

TABLE 1. - Original data published by Jolly

	Gew. d. Kolbens 0°		Kolben 0° 0.02 mm	Gew. d. 0 0°		Gew. d. 0 0° 760 mm
	Bar.	K = T+	K = T-	Bar.	Gew.	
I	714.45	0.083799	1.272183	714.43	1.355982	1.442470
II	711.30	0.077913	1.272187	711.28	1.350100	1.442579
III	715.02	0.074904	1.272180	715.00	1.347084	1.442489
IV	720.42	0.095182	1.272224	720.40	1.367406	1.442570
V	722.02	0.098103	1.272380	722.000	1.370483	1.442571
VI	706.93	0.069659	1.272188	706.91	1.341847	1.442562
VII	693.79	0.044552	1.272222	693.77	1.316774	1.442478
				Mittel		1.442545

The second column, headed Bar., is evidently the barometric pressure reduced to mm of Hg at 0° C under local gravity conditions. The third column gives the weight that must be added to the tare to balance the globe filled with oxygen to a pressure equal to the barometric pressure. The fourth column gives the weights that must be added to the evacuated globe to balance the tare. These are the data that I have called M_{w_1} and M_{w_2} .

Evidently, column 6 is nothing but the sum of columns 3 and 4, that is $M_{w_1} + M_{w_2}$.

The fifth column is the barometric pressure minus 0.02 mm, which was the pressure when the globe was evacuated.

Column seven is evidently column six times 760, divided by the pressure listed in column five. In table 2, I give this number calculated from columns five and six and compare it with Jolly's value given in column seven.

TABLE 2. - Comparison of calculated data

	ΔP	$M_{w_1} + M_{w_2}$	$(M_{w_1} + M_{w_2}) \frac{760}{\Delta P}$	Jolly	Δ
I	714.43	1.355982	1.442473	1.442470	+.000003
II	711.28	1.350100	1.442577	1.442579	-.000002
III	715.00	1.347084	1.431866	1.442489	-.010623
IV	720.40	1.367406	1.442572	1.442570	+.000002
V	722.00	1.370483	1.442614	1.442571	+.000043
VI	706.91	1.341847	1.442622	1.442562	+.000060
VII	693.77	1.316774	1.442478	1.442478	.000000

Evidently there is a typographical error in connection with experiment III and possibly with experiments V and VI.

If $M_{w_1} + M_{w_2} = 1.357084$ for experiment III, then

(12). These values must be corrected for the air buoyancy on the

platinum weights or $(M_{w_1} + M_{w_2}) 760$ correction of the globe,

$$\frac{(M_{w_1} + M_{w_2}) 760}{715.00} = 1.442495.$$

For the buoyancy correction, I have used the density of air

as 0.0012 g/ml and the density of platinum as 21.45 g/ml. The
This is to be compared with Jolly's tabulated value of 1.442489.

Factor

This is sufficiently close to my calculated value that for experiment III, I take $M_{w_1} = 0.084904$.

I then find the values given in table 3.

TABLE 3. - Accepted values of $M_{w_1} + M_{w_2}$

	$M_{w_1} + M_{w_2}$	$(M_{w_1} + M_{w_2}) \frac{760}{\Delta P}$	Jolly
I	1.355982	1.442473	1.442470
II	1.350100	1.442577	1.442579
III	1.357084	1.442495	1.442489
IV	1.367406	1.442572	1.442570
V	1.370483	1.442614	1.442571
VI	1.341847	1.442622	1.442562
VII	1.316774	1.442478	1.442478
Mean		1.4425473	1.4425313

(11) Soles, L. and R. Alvarado

At the bottom of table 3, I give the mean of the values calculated by me and the mean of the values tabulated by Jolly. However, Jolly gives the mean of the values tabulated by him as 1.442545.

This essentially agrees with the mean of my calculated values and not with the mean of his tabulated values. I have therefore concluded that the values given in column 2 in table 3 are the values to

be used in calculating the weight of oxygen, $g_1 - g_2$ of equation (12). These values must be corrected for the air buoyancy on the platinum weights and for the contraction of the globe.

For the buoyancy correction, I have taken the density of air as 0.0012 g/ml and the density of platinum as 21.45 g/ml. The factor

$$1 - \frac{\rho_{\text{air}}}{\rho_w} = 1 - \frac{0.0012}{21.45} = 0.99994406 \quad (14)$$

where V is the volume of the flask in ml and must be multiplied by each of the values of $(M_{w_1} + M_{w_2})$ listed in table 3. w is the weight of the flask in grams

table 3. Flasks

In order to make the correction for the contraction of the globe, it is necessary to know the value of β , used in equations (10) and (12). This coefficient has been determined by Moles and Miravalles (11) (12),

(11) Moles, E. and R. Miravalles

A Cerca de la Compresibilidad de los Matraces vacios en la Determination de gases (The Compressibility of Evacuated Flasks in the Determination of Gas Densities) Anales de la Sociedad Espanola de fisica y quimica, v. 20, 1922, pp. 104-116.

54.7 is the value assumed by the globe in the flask. I have

(12) Moles, E. and R. Miravalles ^{ing minus the pressure given in}
 Sur la Contraction des Ballons Vides dans les Mesures de la
 Densité de Gas (On the Contraction of Empty Flasks in Measure-
 ment of gas Densities) J. de Chemie Physique, v. 21, 1924,
 pp. 1-9.

who made measurements on many different globes. They give

$$\beta (\text{atm}^{-1}) = \frac{V}{w} \times 15.5 \times 10^{-6} \quad (14)$$

where V is the volume of the flask in ml and

w is the weight of the flask in grams

For Jolly's flask

$$V = 1009.42 \text{ ml}$$

$$w = 142.12 \text{ gm}$$

$$V/w = 7.103$$

So that

$$\beta = 1.101 \times 10^{-4} (\text{atm}^{-1})$$

Since this correction is a small correction, I have taken

$V_o (1 + \alpha t_2)$ in equation (12) as being ^{as, while Moles (14)}

$$V_o (1 + \alpha t_2) = 1009.4 + 54.7$$

Etude Critique des Valeurs = 1064.1 ml. de Densité du gaz—
 Oxygène (Critical Study of Modern Values of the Density of
 Oxygen Gas) Journal de Chimie Physique et Physique Générale des
 Colloïdes, v. 19, 1921, pp. 100-120.

54.7 is the volume occupied by the glass in the flask. I have estimated it to be 0.0001 which in a later paper by Moles and taken ΔP_2 in equation (12) as being minus the pressure given in column 2 of table 2, divided by 760.

The calculations of the weights of oxygen are summarized in table 4. $g_1 - g_2$ was calculated using equation (12).

TABLE 4. - Calculation of mass of oxygen

	$(M_{w_1} + M_{w_2})(1 - \frac{\rho_{air}}{\rho_w})$	$-V_o(1 + \alpha t_2) \beta \Delta P_2 \rho_{air}$	$g_1 - g_2$
I	1.355906	0.000132	1.356038
II	1.350024	0.000132	1.350156
III	1.357008	0.000132	1.357140
IV	1.367330	0.000133	1.367463
V	1.370406	0.000134	1.370540
VI	1.341772	0.000131	1.341903
VII	1.316700	0.000128	1.316828

The values of the correction for the contraction of the globe, a atmosphere is defined as 760 mm of Hg at $0^\circ C$ under the conditions represent a correction of 0.00014 in the final value of the density of oxygen. Lord Rayleigh (13)

(13) Reference 10, page 147

estimated this correction to be 0.00032, while Moles (14)

(14) Moles, E.

Etude Critique des Valuers Modernes de la Densite du gaz Oxygene (Critical Study of Modern Values of the Density of Oxygen Gas) Journal de Chimie Physique et Revue Generale des Colloides, v. 19, 1921, pp. 100-120.

estimated it to be 0.00020, which in a later paper by Moles and Gonzalez (15),

(15) Moles, E. and F. Gonzalez

Nouvelle Revision de la Densite Normale du Gaz Oxygene. (New Revision of the Normal Density of Oxygen Gas.) Journal de Chimie Physique, v. 19, 1921, pp. 310-323. Footnote 2 on page 322.

was changed to 0.00016.

CALCULATION OF THE DENSITY OF OXYGEN

In this section I derive the formula necessary to calculate the density of oxygen at 0° C and at 1 atmosphere where in this section, 1 atmosphere is defined as 760 mm of Hg at 0° C under the conditions of local gravity.

In each experiment, the globe contained g_1 grams of oxygen at a pressure P_1 , near 1 atmosphere and at a volume V_o . When evacuated to the pressure P_2 , the globe contained g_2 grams of oxygen, in the volume V_2 where

$$V_2 = V_o [1 + \frac{g}{M} (P_2 - P_1)] \quad (15)$$

I apply the exact equations

$$P_1 V_o = \frac{g_1 R T_o Z_1}{M} \quad (16)$$

$$P_2 V_2 = \frac{g_2 \frac{RT}{M} Z_2}{P_1} = P_2 V_0 [1 + \beta(P_2 - P_1)] \quad (17)$$

where M is the molecular weight of oxygen and Z is the compressibility factor. Then

$$\frac{P_1}{P_2} = \frac{g_1 Z_1}{g_2 Z_2} [1 + \beta(P_2 - P_1)] \quad (18)$$

or finally

$$g_2 = g_1 \frac{Z_1}{Z_2} \frac{P_2}{P_1} [1 + \beta(P_2 - P_1)] \quad (19)$$

Thus

$$g_1 - g_2 = g_1 \left(1 - \frac{Z_1}{Z_2} \frac{P_2}{P_1} [1 + \beta(P_2 - P_1)] \right) \quad (20)$$

Equation (20) shows that the weight of oxygen, that would fill Jolly's globe at a pressure of 760 mm Hg at $0^\circ C$, to be calculated.

and

$$g_1 = \frac{g_1 - g_2}{1 - \frac{Z_1}{Z_2} \frac{P_2}{P_1} [1 + \beta(P_2 - P_1)]} \quad (21)$$

the compressibility factor at $0^\circ C$ to be given by

Now let g_{760} be the grams of oxygen that would be in the globe at a pressure of 760 mm of Hg at $0^\circ C$ and with the barometric pressure the same. With P_{760} representing this pressure, we have

$$\frac{P_1}{P_{760}} = \frac{g_1}{g_{760}} \frac{Z_1}{Z_{760}} \quad (22)$$

The details of the calculation of g_{760} are summarized in table 5.

$$g_{760} = g_1 \frac{z_1}{z_{760}} \frac{p_{760}}{p_1} \quad (23)$$

and substituting for g_1 from equation (21), we have

$$g_{760} = \frac{(g_1 - g_2) \frac{z_1}{z_{760}} \frac{p_{760}}{p_1}}{1 - \frac{z_1}{z_2} \frac{p_2}{p_1} [1 + \beta(p_2 - p_1)]} \quad (24)$$

and finally

$$g_{760} = \frac{(g_1 - g_2) p_{760}}{p_1 - \frac{z_1}{z_2} p_2 [1 + \beta(p_2 - p_1)]} \frac{z_1}{z_{760}} \quad (25)$$

calculated value is higher by a factor 1.00010. This is principally due to the use of 760 mm Hg as the standard pressure. Equation (25) allows the mass of oxygen, that would fill Jolly's globe at a pressure of 760 mm Hg at 0° C, to be calculated.

Jolly assumed all of the compressibility factors were equal to one. For making the compressibility correction, I have assumed the compressibility factor, at 0° C to be given by

$$z = 1 - 0.000965 \frac{p}{760} \quad (26)$$

TABLE 4. - Density of oxygen at 0° C, the use of Hg, local gravity

With the pressure in mm of Hg at 0° C, β is given by

$$\beta = \frac{0.0001101}{760} = 1.45 \times 10^{-7} (\text{mm Hg})^{-1}$$

The details of the calculations of g_{760} are summarized in table 5.

REDUCTION OF THE DENSITY OF OXYGEN TO GRAVITY OF 980.616 CM/SEC²

TABLE 5. - Calculation of mass of oxygen needed to fill Jolly's globe at 0°C and 760 mm of Hg at local gravity

	P_1	$g_1 - g_2$	Z_1/Z_{760}	g_{760}
I	714.45	1.356038	1.0000579	1.4426165
II	711.30	1.350156	1.0000619	1.4427259
III	715.02	1.357140	1.0000572	1.4426369
IV	720.42	1.367463	1.0000503	1.4427042
V	722.02	1.370540	1.0000482	1.4427432
VI	706.93	1.341903	1.0000675	1.4427793
VII	693.79	1.316828	1.0000842	1.4426590
			Mean	1.4426950 g

The mean for g_{760} given by Jolly is 1.442545 which means my calculated value is higher by a factor 1.00010. This is principally due to the neglect, by Jolly, of the compressibility factor, Z/Z_{760} , and the contraction of the globe.

Using a value of 1.0094221 liters for the volume of Jolly's globe, the values of the density of oxygen at 0°C and under a pressure of 760 mm Hg at 0°C and local gravity were calculated. These values are given in table 6.

TABLE 6. - Density of oxygen at 0°C, 760 mm of Hg, local gravity

	ρ , g/l
I	1.4291509
II	1.4292593
III	1.4291711
IV	1.4292378
V	1.4292764
VI	1.4293122
VII	1.4291930
Mean	1.429229 ± 22

given. The plus or minus is the standard deviation of the mean.

REDUCTION OF THE DENSITY OF OXYGEN TO GRAVITY OF 980.616 CM/SEC²

(17) Ph. v. Jolly gives for his laboratory in Munich,

Tables for the latitude = 48° 8' according to the New International Forme

elevation = 515 meters

Woppard and Rose (16) 1961, pp. 327-340.

(16) Woppard, George P. and John C. Rose

International Gravity Measurements. Published by Society of
Exploration Geophysicists, October 1963, 518pp., Composed and
Printed by George Banta Company, Inc. Menasha, Wisconsin,

(18) p. 514. National Critical Tables, v. 1, 1926, p. 602, McGraw-

give for the acceleration of gravity, at Munich, in the Potsdam
system for the Residenz station

$$g = 980.7384 \text{ cm/sec}^2$$

with

To correct for the latitude = 48° 8.5' N, to 760 mm of Hg.

with $g = 980.616 \text{ cm/sec}^2$ longitude = 11° 34.9' E

elevation = 510 meters

The change in g from a latitude of 48° 8.5' to 48° 8' is

given by Lambert and Darling's tables (17)

(17) Lambert, W. D., and F. W. Darling

Tables for Theoretical Gravity According to the New International Formula, Bulletin Geodesique Organe de la Section de Geodesie, No. 32, 1931, pp. 327-340.

as -0.00075.

The change in g from an elevation of 510 meters to an elevation of 515 meters is given by (18)

(18) International Critical Tables, v. 1, 1926, p. 402, McGraw-Hill Book Company, Inc., New York, 370 Seventh Avenue.

$$-0.0003086 \times 5 = -0.00154.$$

Thus for Ph. v. Jolly's laboratory

$$g = 980.7384 - .00075 - .00154$$

$$g = 980.7361 \text{ cm/sec}^2.$$

To correct the values given in table 6, to 760 mm of Hg, with $g = 980.616$, we must multiply by

Indicate should be done.

The fourth column of table 7 gives the ratio of the densities calculated by Moles to those calculated by Moller. The values differ by almost 100 parts per million (ppm). This difference is principally due to the fact that Moles applied a buoyancy

correction to the weights in the determination of the mass of oxygen, but he assumed the weights were of brass with a density

TABLE 7. - Density of oxygen at 0° C, 760 mm of Hg,
gravity = 980.616 cm/sec²

	ρ g/l	ρ g/l (Moles 1921)	Ratio
I	1.4289759	1.42885	1.000088
II	1.4290843	1.42895	1.000094
III	1.4289961	1.42887	1.000088
IV	1.4290628	1.42893	1.000093
V	1.4291014	1.42898	1.000085
VI	1.4291372	1.42901	1.000089
VII	<u>1.4290180</u>	1.42886	1.000111
Mean	1.429054 \pm 22		

The third column of table 7 gives the values calculated by

Moles (19),

(19) Reference 14, page 103.

decreased by 0.00004, as Moles and Gonzalez (20)

(20) Reference 15, page 322, Footnote 2.

indicate should be done.

The fourth column of table 7 gives the ratio of the densities calculated by me to that calculated by Moles. The values differ by almost 100 parts per million (ppm). This difference is principally due to the fact that Moles applied a buoyancy

correction to the weights in the determination of the mass of oxygen, but he assumed the weights were of brass with a density of 8.4, while I assumed they were platinum with a density of 21.45. This leads to a difference of 87 ppm.

COMPARISON WITH PREVIOUSLY RECALCULATED
VALUES OF THE DENSITY OF OXYGEN

In Internal Report No. 44 (21)

(21) Barieau, Robert E.

Recalculation of the Work of V. Regnault on the Density of Oxygen. Helium Research Center Internal Report No. 44, November 1963.

I recalculated the work of V. Regnault (22)

(22) Regnault, V. Deuxieme Memoire. Sur la Determination de la Densite des gaz, pp. 121-150. Troisieme Memoire. Determination du Poids d air et de la Densite du Mercure, pp. 151-162. Memories de l' Academie Royal des Sciences de l' Institute de France, v. XXI, 1847.

on the density of oxygen. The comparison of the density of

oxygen follows:

Author	ρ g/l
Regnault, Paris, 1847	1.429626 \pm 22
Jolly, Munich, 1879	1.429054 \pm 22

This is the density of oxygen in grams per liter, at 0° C and a pressure of 1 atmosphere, where 1 atmosphere is 760 mm of Hg at 0° C in a gravitational field of 980.616 cm/sec² in the Potsdam system.

Fig. 9. *Leptothrix* sp. nov.

Fig. 9
 $22 \pm 33.0254.1$
 $22 \pm 40.0054.1$

1973A
Leptothrix sp. nov.
Tolliyimuk, 1973

Fig. 9. *Leptothrix* sp. nov. is a genus of bacteria in the family Leptothrixidae. It is a Gram-negative, rod-shaped bacterium with a peritrichous flagella. It is found in soil and water environments. The type species is *Leptothrix pallens* (Bacillus pallens) and it has a G+C content of 51.0-52.0%. The genus was first described in 1973 by Tolliyimuk.

Published by the author.

